Exotic features of superfluid dynamics



Piotr Magierski Warsaw University of Technology (WUT)

Collaborators:

Matthew Barton (WUT) Konrad Kobuszewski (WUT - Ph.D. student) Daniel Pęcak (WUT) <u>Kazuyuki Sekizawa (WUT -> Niigata U.)</u> <u>Buğra Tüzemen (WUT - Ph.D. student)</u> Marek Tylutki (WUT) <u>Gabriel Wlazłowski (WUT)</u>

Pairing induced quantized states

Scattering of particles/holes on the pairing potential:





Superconductor

Andreev reflection law:

$$\sqrt{\varepsilon_F + E} \sin \alpha = \sqrt{\varepsilon_F - E} \sin \beta$$

Consequences:

Andreev reflection gives rise to the appearance of localized quantized states - *Andreev states*.

Due to the properties of Andreev reflection "shell effects" induced by Andreev states are quite strong (Andreev reflection effectively reduces 3D problem to 1D problem)

Andreev reflection provides an effective mechanism to *localize states* at the Fermi surface in <u>inhomogenous systems</u>. (see: P. Magierski, Phys. Rev. C75, 012803(R), 2007)

It generates strong <u>Casimir-like force</u> between superfluid grains. (see: A.Bulgac, P. Magierski, A. Wirzba, Eur. Lett.72,327,2005)

Pairing in spin imbalanced superfluids

Clogston-Chandrasekhar condition sets the limit for the chemical potential difference at which superfluidity is lost: $|\mu_{\downarrow} - \mu_{\uparrow}| \propto \Delta$



K.B. Gubbels, H.T.C. Stoof / Physics Reports 525 (2013) 255-313

Inhomogeneous systems: Fulde-Ferrell-Larkin-Ovchinnikov (FFLO) phase

Larkin-Ovchinnikov (LO): $\Delta(r) \sim cos(\vec{q} \cdot \vec{r})$ Fulde-Ferrell (FF): $\Delta(r) \sim \exp(i\vec{q} \cdot \vec{r})$

A.I. Larkin and Y. N. Ovchinnikov, Sov. Phys. JETP 20, 762 (1965) P. Fulde and R. A. Ferrell, Phys. Rev. 135, A550 (1964)

Spatial modulation of the pairing field cost energy proportional to q^2 but may be compensated by an increased pairing energy due to the mutual shift of Fermi spheres:



A. Bulgac, M.M.Forbes, Phys. Rev. Lett. 101,215301 (2008) See also review of mean-field theories : Radzihovsky,Sheehy, Rep.Prog. Phys.73,076501(2010)

Andreev states and stability of pairing nodal points



Due to quasiparticle scattering the localized Andreev states appear at the nodal point. These states induce local spin-polarization

BdG in the Andreev approx. (
$$\Delta \ll k_F^2$$
)

$$\begin{bmatrix} -2ik_F \frac{d}{dx} & \Delta(x) \\ \Delta^*(x) & 2ik_F \frac{d}{dx} \end{bmatrix} \begin{bmatrix} u_{n\uparrow}(x) \\ v_{n\downarrow}(x) \end{bmatrix} = E_n \begin{bmatrix} u_{n\uparrow}(x) \\ v_{n\downarrow}(x) \end{bmatrix}$$

Another perspective: superconductor-ferromagnet junction



Engineering the structure of nodal surfaces

Apply the spin-selective potential of a certain shape:



Wait until the proximity effects of the pairing field generate the nodal structure and remove the potential.

For example the spherical nodal structure:

Important!

Nodal structure is **unstable** without spin-polarization. And vice versa: **spin-polarization** (ie. excess of the majority spin particles) is expelled from superfluid unless pairing nodal structure is created.





Contraction of the nodal sphere is prevented by the pairing potential barrier. Expansion of the nodal sphere will cost the energy due to expansion of polarized shell.

As a result of the interplay between volume and surface energies keeps the impurity stable

P. Magierski, B.Tüzemen, G.Wlazłowski, Phys. Rev. A (in press), arXiv:1811.00446



Moving impurity:

From Larkin-Ovchinnikov towards Fulde-Ferrell limit:

 $\Delta(r): cos(\vec{q} \cdot \vec{r}) \Longrightarrow \exp(i\vec{q} \cdot \vec{r})$

Surprisingly, the nodal structure remains stable even during collisions

The velocities of impurites are about 30% of the velocity of sound.



Summary of the first part

It is possible to create dynamically <u>stable</u>, <u>locally spin-polarized</u> region in the ultracold Fermi gas.

The stability is due to the peculiar pairing structure characteristic for the FFLO phase.

The conditions of stability:

- <u>do not depend</u> on details of the functional (simple BdG approach predicts qualitatively the same results)
- <u>do not depend</u> whether we are on the BEC-side (a>0) or on the BCS-side (a<0), although UFG may be the best system for experimental realization.

The effect can be viewed as:

- long-lived, spin-polarized excitation mode of UFG
- <u>FFLO droplet</u> (although its size is of few coherence lengths only)

We dubbed it *ferron*

How about unstable nodal structures?



Unstable pairing nodal structures: nuclear collisions

Collisions of superfluid nuclei having <u>different phases</u> of the <u>pairing fields</u>

The main questions are:

-how a possible solitonic structure can be manifested in nuclear system? -what observable effect it may have on heavy ion reaction: kinetic energy distribution of fragments, capture cross section, etc.?

Clearly, we cannot control phases of the pairing field in nuclear experiments and the possible signal need to be extracted after averaging over the phase difference.



Estimates for the magnitude of the effect

At first one may think that the magnitude of the effect is determined by the nuclear pairing energy which is of the order of MeV's in atomic nuclei (according to the expression): $\frac{1}{2}$

 $\frac{1}{2}g(\varepsilon_F)|\Delta|^2$; $g(\varepsilon_F)$ - density of states

On the other hand the energy stored in the junction can be estimated from Ginzburg-Landau (G-L) approach:



For typical values characteristic for two medium nuclei: $E_i \approx 30 MeV$



Creation of <u>the solitonic structure</u> between colliding nuclei prevents energy transfer to internal degrees of freedom and consequently <u>enhances</u> the kinetic energy of outgoing fragments. Surprisingly, the <u>gauge angle dependence</u> from the G-L approach is perfectly well reproduced in <u>the kinetic energies of outgoing fragments</u>! Effective barrier height for fusion as a function of the phase difference



What is an average extra energy needed for the capture?

$$E_{extra} = \frac{1}{\pi} \int_{0}^{\pi} \left(B\left(\Delta\varphi\right) - V_{Bass} \right) d\left(\Delta\varphi\right) \approx 10 MeV$$

The effect is found (within TDDFT) to be of the order of <u>30MeV</u> for medium nuclei and occur for <u>energies up to 20-30% of the barrier height</u>.

P. Magierski, K. Sekizawa, G. Wlazłowski, Phys. Rev. Lett. 119 042501 (2017)

It raises (again) an interesting (and well known) question: to what extent systems of hundreds of particles can be described using the concept of pairing field?

G. Scamps, Phys. Rev. C 97, 044611 (2018): barrier fluctuations extracted from experimental data indicate that the effect exists although is weaker than predicted by TDDFT

For recent results on pairing dynamics in nuclear collisions see the poster of Matthew Barton

Suggestion for experimental protocol for ultracold atomic gas:



Two crossing beams: $A = 1\varepsilon_F$, $\sigma = 3.14\xi$



P.Magierski, B.Tüzemen, G.Wlazłowski, Phys. Rev. A (in press) arXiv:1811.00446