## Nuclear reactions within the framework of time dependent density functional theory.



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## GOAL:

Description of <u>superfluid dynamics</u> of fermionic systems <u>far from equilibrium</u> based on microscopic theoretical framework.

Microscopic framework = explicit treatment of fermionic degrees of freedom.

## Why Time Dependent Density Functional Theory (TDDFT)?

We need to describe the time evolution of (externally perturbed) spatially inhomogeneous, superfluid Fermi system.

Within current computational capabilities TDDFT allows to describe real time dynamics of strongly interacting, superfluid systems of <u>hundred of thousands</u> fermions.

#### **TDDFT equations with local pairing field (TDSLDA):**

$$i\hbar\frac{\partial}{\partial t} \begin{pmatrix} u_{k\uparrow}(\mathbf{r},t) \\ u_{k\downarrow}(\mathbf{r},t) \\ v_{k\uparrow}(\mathbf{r},t) \\ v_{k\downarrow}(\mathbf{r},t) \end{pmatrix} = \begin{pmatrix} h_{\uparrow,\uparrow}(\mathbf{r},t) & h_{\uparrow,\downarrow}(\mathbf{r},t) & 0 & \Delta(\mathbf{r},t) \\ h_{\downarrow,\uparrow}(\mathbf{r},t) & h_{\downarrow,\downarrow}(\mathbf{r},t) & -\Delta(\mathbf{r},t) & 0 \\ 0 & -\Delta^*(\mathbf{r},t) & -h^*_{\uparrow,\uparrow}(\mathbf{r},t) & -h^*_{\uparrow,\downarrow}(\mathbf{r},t) \\ \Delta^*(\mathbf{r},t) & 0 & -h^*_{\uparrow,\downarrow}(\mathbf{r},t) & -h^*_{\downarrow,\downarrow}(\mathbf{r},t) \end{pmatrix} \begin{pmatrix} u_{k\uparrow}(\mathbf{r},t) & u_{k\downarrow}(\mathbf{r},t) \\ u_{k\downarrow}(\mathbf{r},t) \\ v_{k\uparrow}(\mathbf{r},t) \\ v_{k\downarrow}(\mathbf{r},t) \end{pmatrix}$$

#### The form of h(r,t) and $\Delta(r,t)$ is determined by EDF (Energy Density Functional)

- •The system is placed on a large 3D spatial lattice.
- No symmetry restrictions.
- Number of PDEs is of the order of the number of spatial lattice points.

*Table 1: Comparison of profit gained by using GPUs instead of CPUs for two example lattices. The timing was obtained on Titan supercomputer. Note, Titan has 16x more CPUs than GPUs.* 

	<b>CPU</b> impleme	ntation	GPU impleme	ntation	
Number of H	FB				
N <sub>x</sub> N <sub>y</sub> N <sub>z</sub> equatio	ns # of CPUs	time per step	# of GPUs	time per step	SPEEDUP
48 <sup>3</sup> 110,5	592 110,592	3.9 sec	6,912	0.39 sec	10
64 <sup>3</sup> 262,1	.44 262,144	20 sec	16,384	0.80 sec	25

The main advantage of TDSLDA over TDHF (+TDBCS) is related to the fact that in TDSLDA the pairing correlations are described as a true <u>complex field which has its own modes of excitations</u>, which include spatial variations of both amplitude and phase. Therefore in TDSLDA description the evolution of nucleon Cooper pairs is treated consistently with other one-body degrees of freedom.

## **Advantages of TDDFT**

- The same framework describes various limits: eg. <u>linear and highly nonlinear</u> regimes, <u>adiabatic and nonadiabatic (dynamics far from equilibrium)</u>.
- TDDFT <u>does not require</u> introduction of hard-to-define <u>collective degrees of</u> <u>freedom</u> and there are no ambiguities arising from defining <u>potential energy</u> <u>surfaces and inertias</u>.
- <u>One-body dissipation, the window and wall dissipation mechanisms</u> are automatically incorporated into the theoretical framework.
- All shapes are allowed and the nucleus chooses dynamically the path in the shape space, the forces acting on nucleons are determined by the nucleon distributions and velocities, and <u>the nuclear system naturally and smoothly</u> <u>evolves into separated fission fragments</u>.
- There is no need to introduce such unnatural quantum mechanical concepts as "rupture" and there is <u>no worry about how to define the scission configuration</u>.



## **Areas of applications**



Ultracold atomic (fermionic) gases. Unitary regime. Dynamics of quantum vortices, solitonic excitations, quantum turbulence.





 $\frac{\Delta}{-} \leq 0.1 - 0.2$  $\mathcal{E}_{F}$ 

Astrophysical applications. Modelling of neutron star interior (glitches): vortex dynamics, dynamics of inhomogeneous nuclear matter (in strong magnetic fields).





Nuclear physics. Induced nuclear fission, fusion, collisions.





**Examples of applications:** 

- Nuclear induced fission
- Collisions of medium or heavy superfluid nuclei

## Fission dynamics of <sup>240</sup>Pu

Initial configuration of  ${}^{240}Pu$  is prepared beyond the barrier at quadrupole deformation Q=165b and excitation energy E=8.08 MeV: Accelerations in quadrupole and octu-



Accelerations in quadrupole and octupole moments along the fission path



Note that despite the fact that nucleus is already <u>beyond the saddle point</u> the collective motion on the time scale of 1000 fm/c and larger is characterized by <u>the constant velocity</u> (*see red dashed line for an average acceleration*) till the very last moment before splitting. On times scales, of the order of 300 fm/c and shorter, the collective motion is a subject to random-like kicks indicating strong coupling to internal d.o.f



#### Induced fission of 240Pu

The lighter fragment is more excited (and strongly deformed) than the heavier one.

# Energies are not shared proportionally to mass numbers of the fragments!

TKE = 17	77.80 -	$0.3489E_{n}$	[in MeV],
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Nuclear data evaluation, Madland (2006)

Calculated TKEs slightly underestimate the observed values by no more than: 1 - 3 MeV !

J. Grineviciute, et al. (in preparation) see also:

A. Bulgac, P. Magierski, K.J. Roche, and I. Stetcu, Phys. Rev. Lett. 116, 122504 (2016)

### Nuclear collisions

Collisions of superfluid nuclei having <u>different phases</u> of the <u>pairing fields</u>

Inspired by experiments on ultracold atomic gases: merging two 6Li clouds





Creation of a "<u>heavy soliton</u>" after merging two superfluid atomic clouds. T. Yefsah et al., Nature 499, 426 (2013).

And recently detailed analysis of **solitonic cascade** has been performed in experiment at MIT: M.J.H. Ku et al. Phys. Rev. Lett. 116, 045304 (2016)

Wlazłowski, Sekizawa, Magierski (in preparation)

<u>In the context of nuclear systems the main questions are:</u> -how a possible solitonic structure can be manifested in nuclear system? -what observable effect it may have on heavy ion reaction: kinetic energies of fragments, capture cross section, etc.?

Clearly, we cannot control phases of the pairing field in nuclear experiments and the possible signal need to be extracted after averaging over the phase difference.



Y. Hashimoto, G. Scamps, Phys. Rev. C94, 014610(2016) – TDHFB studies of small systems: 200+200 reaction produced negligible effect.

#### Ultracold atomic gases: two regimes for realization of the Josephson junction

Weak coupling (weak link)

Strong coupling

Time

200 µm



between two 6Li atomic cloud It need not to be accompanied creation of a topological excitation

G. Valtolina et al., Science 350, 1505 (2015

Creation of a "heavy soliton" after merging two superfluid atomic clouds.

T. Yefsah et al., Nature 499, 426 (2013).

## Estimates for the magnitude of the effect

At first one may think that the magnitude of the effect is determined by the nuclear pairing energy which is of the order of MeV's in atomic nuclei (according to the expression):

$$\frac{1}{2}g(\varepsilon_F)|\Delta|^2$$
;  $g(\varepsilon_F)$  - density of states

On the other hand the energy stored in the junction can be estimated from Ginzburg-Landau (G-L) approach:

For typical values characteristic for two heavy nuclei:  $E_i \approx 30 MeV$ 

# $^{240}Pu + ^{240}Pu$ at energy $E \simeq 1.1V_{Bass}$







Creation of <u>the solitonic structure</u> between colliding nuclei prevents energy transfer to internal degrees of freedom and consequently <u>enhances</u> the kinetic energy of outgoing fragments. Surprisingly, the <u>gauge angle dependence</u> from the G-L approach is perfectly well reproduced in <u>the kinetic energies of outgoing fragments</u>!





Effective barrier height for fusion as a function of the phase difference



What is an average extra energy needed for the capture?

$$E_{extra} = \frac{1}{\pi} \int_{0}^{\pi} \left( B\left(\Delta\varphi\right) - V_{Bass} \right) d\left(\Delta\varphi\right) \approx 10 MeV$$

How the angle dependence affects the shape of the excitation function?

$$\frac{d}{dE} \left( E \sigma(E) \right) \propto \Delta \varphi_{tr} + \dots$$

#### <u>Summarizing</u>

<u>Pairing field dynamics play an important role in nuclear dynamics including both</u> induced fission and collisions.

Clearly the aforementioned effects CANNOT be grasped by any version of simplified (and commonly used) TDHF+BCS approach.

The phase difference of the pairing fields of colliding medium or heavy nuclei produces a similar <u>solitonic structure</u> as the system of two merging atomic clouds.

The energy stored in the created junction is subsequently released giving rise to an increased kinetic energy of the fragments and modifying their trajectories. The effect is found to be of the order of <u>30MeV</u> for heavy nuclei and occur for energies up to 20-30% of the barrier height.

Consequently the effective barrier for the capture of medium nuclei is enhanced by about <u>10MeV</u>.

Josephson current is weak and <u>DOES NOT</u> contribute noticeably to collision dynamics (consistent with other studies).

#### **Open question**

Time dependent DFT describes nuclear collision in <u>the broken symmetry</u> <u>framework.</u>

What is the effect of the particle nonconservation?

Whether the broken symmetry framework provides a reasonable description depends on the <u>time scale</u> associated with the related Goldstone mode.

Here, the time scale is related to the inverse of the neutron separation energy. However, since both pairing fields rotate in gauge space it is rather the difference of the separation energy which matters (this can be made <u>arbitrarily</u> <u>long</u> in the case of <u>symmetric collisions</u>).

For discussion of phase-locking in the strong coupling limit see also: A. Bulgac, Shi Jin, Phys. Rev. Lett. 119, 052501 (2017)

## Summarizing

- TDDFT extended to superfluid systems and based on the local densities offers a flexible tool to study quantum superfluids far from equilibrium.
- TDDFT offers an unprecedented opportunity to test the nuclear energy density functional for large amplitude collective motion, nonequilibrium phenomena, and in new regions of the collective degrees of freedom.
- Interesting research topics:
- Ultracold atoms: investigation of <u>quantum turbulence</u> in Fermi systems; topological excitations in <u>spin-polarized</u> atomic gases in the presence of <u>LOFF phase</u>.
  Neutron star: Provide a link between <u>large scale models</u> of neutron stars and microscopic studies; towards the first simulation of the <u>glitch phenomenon</u> based on microscopic input.
  Nuclear physics: induced fission and fusion processes based directly on Energy Density Functional; search for new effects related to <u>pairing dynamics</u> in <u>nuclear processes</u>.